

Table of Laplace Transforms and Inverse Transforms

$f(t) = \mathcal{L}^{-1}\{F(s)\}(t)$	$F(s) = \mathcal{L}\{f(t)\}(s)$
$t^n e^{at}$	$\frac{n!}{(s-a)^{n+1}}, \quad s > a$
$e^{at} \sin bt$	$\frac{b}{(s-a)^2 + b^2}, \quad s > a$
$e^{at} \cos bt$	$\frac{s-a}{(s-a)^2 + b^2}, \quad s > a$
$e^{at} f(t)$	$F(s) _{s \rightarrow s-a}$
$u(t-a)f(t)$	$e^{-as} \mathcal{L}\{f(t+a)\}(s)$, alternatively,
$u(t-a)[f(t) _{t \rightarrow t-a}]$	$e^{-as} F(s)$
$\delta(t-a)f(t)$	$f(a)e^{-as}$
$f^{(n)}(t)$	$s^n F(s) - s^{n-1}f(0) - \dots - f^{(n-1)}(0)$
$t^n f(t)$	$(-1)^n \frac{d^n}{ds^n} F(s)$, with special case $\mathcal{L}^{-1}\{F(s)\}(t) = -\frac{1}{t} \mathcal{L}^{-1}\{F'(s)\}(t)$
$\frac{f(t)}{t}$	$\int_s^\infty F(\sigma) d\sigma$, with special case $\mathcal{L}^{-1}\{F(s)\}(t) = t \mathcal{L}^{-1}\left\{\int_s^\infty F(\sigma) d\sigma\right\}(t)$
$\int_0^t f(\tau) d\tau$	$\frac{F(s)}{s}$
$f(t) * g(t)$	$F(s)G(s)$