

1. Evaluate the following:

(a)  $\frac{d}{dx} \int_5^{x^2+e^x} \sin^2(x) dx.$

(b)  $\int \tan(x) dx.$

(c)  $\int_0^3 |2x - 3| dx.$

(d)  $\int_0^{\pi/4} \frac{1 - \sin^2(\theta)}{\cos^2(\theta)} d\theta.$

2. A solid is formed by adjoining two hemispheres to the ends of a right circular cylinder. Find the dimensions that minimize the cost if the volume must be  $300\text{ft}^3$  and the hemispherical ends cost twice as much per square foot of surface area as the sides.

3. Consider the sum:

$$\sum_{k=1}^n (k-2)^2.$$

- (a) Find the value of the sum when  $n = 4$  by computing each term.

- (b) Find the value of the sum when  $n = 50$  by using the summation formulas you were given in class.

4. Find the value of  $f(c)$  guaranteed by the Mean Value Theorem for Integrals in the following problem:

$$\int_1^9 \frac{1}{\sqrt{x}(1 + \sqrt{x})^2} dx.$$

5. Find the volume of the solid generated by revolving the region bounded by  $y = x^2$  and  $y = 4x - x^2$  about the line  $y = 6$ .

6. Find the left-hand, right-hand, and midpoint sums for the function  $y = (x - 3)^2$  on the interval  $[1, 3]$  using four equally spaced intervals. What are you approximating, and which of the three is a better estimate for this?

7. Find the total area between the curve  $y = \cos^2(2t)$  and the x-axis on the interval  $[-\pi/2, \pi]$ .