### Math 314/814, Section 1

### Quiz number 3

Show all work. How you get your answer is just as important, if not more important, than the answer itself. If you think it, write it!

Under different conditions, differing proportions of carbon monoxide, carbon dioxide, and atomic hydrogen will combine to form methane and water.

$$CO + CO_2 + H_2 \rightarrow CH_4 + H_2O$$

Find at least two different (not all 0) ways to balance the equation, which use different proportions of CO versus  $CO_2$ .

Introducing variable, we write  $xCO + yCO_2 + zH_2 = uCH_4 + vH_2O$ 

and set the quantities of each element from each side equal.

$$C: x + y = u,$$
 or  $x + y - u = 0$   
 $C: x + 2y = v,$  or  $x + 2y - v = 0$   
 $H: 2z = 4u + 2v,$  or  $2z - 4u - 2v = 0$ 

As an augmented matrix, this is (with variable order x, y, z, u, v)

$$\begin{pmatrix} 1 & 1 & 0 & -1 & 0 & | & 0 \\ 1 & 2 & 0 & 0 & -1 & | & 0 \\ 0 & 0 & 2 & -4 & -2 & | & 0 \end{pmatrix}$$

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$$\begin{pmatrix} 1 & 1 & 0 & -1 & 0 & | & 0 \\ 1 & 2 & 0 & 0 & -1 & | & 0 \\ 0 & 0 & 2 & -4 & -2 & | & 0 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 1 & 0 & -1 & 0 & | & 0 \\ 0 & 1 & 0 & 1 & -1 & | & 0 \\ 0 & 0 & 1 & -2 & -1 & | & 0 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 0 & 0 & -2 & 1 & | & 0 \\ 0 & 1 & 0 & 1 & -1 & | & 0 \\ 0 & 0 & 1 & -2 & -1 & | & 0 \end{pmatrix}$$

So u and v are free, and

$$x = 2u - v$$
$$y = v - u$$
$$z = 2u + v$$

So, for example, setting (noting that  $u \leq v \leq 2u$  gives all non-negative values)

$$u=1, \text{ v=1} \\ yields \\ \textbf{x=1}, y=0, z=2, \qquad \text{and} \qquad CO+2H_2 \rightarrow CH_4 + H_2O$$
 while  $u=1, \text{ v=2} \\ yields \\ \textbf{x=0}, y=1, z=1, \qquad \text{and} \qquad CO2+2H_2 \rightarrow CH_4 + 2H_2O$ 

More interestingly (?), u = 2, v=3yieldsx=1, y = 1, z = 7, and  $CO_2 + CO$  $+7H_2 \rightarrow 2CH_4 + 3H_2O$ 

# Name:

# Math 314/814, Section 5

# Quiz number 3

Show all work. How you get your answer is just as important, if not more important, than the answer itself. If you think it, write it!

Under different conditions, ethane and atomic oxygen will combine (burn) to form differing proportions of carbon monoxide, carbon dioxide, and water.

$$C_2H_6 + O_2 \rightarrow CO + CO_2 + H_2O$$

Find at least two different (not all 0) ways to balance the equation, which create different proportions of CO versus  $CO_2$ .