

MATH 107-253 Recitation 16

JD Nir

Avery 230 • Office Hours: W 4-5 R 11-12

jnir@huskers.unl.edu

www.math.unl.edu/~jnir2/107-253.html

October 22, 2015

1: Find the volume of the solid whose base is the region in the first quadrant bounded by $y = x^2$, $y = 1$, and the y -axis and whose cross-sections perpendicular to the x -axis are semicircles.

2: Find the equation (in terms of x and y) of the tangent line to the curve $r = 2 \sin 4\theta$ at $\theta = \frac{\pi}{3}$.

3: A storage shed is the shape of a half-cylinder of radius r and length l .

(a) What is the volume of the shed?

(b) The shed is filled with sawdust whose density (mass/unit volume) at any point is proportional to the distance of that point from the floor. The constant of proportionality is k . Calculate the total mass of sawdust in the shed.

4: A bucket of water of mass 20 kg is pulled at constant velocity up to a platform 50 meters above the ground. This takes 20 minutes, during which time 4 kg of water drips out at a steady rate through a hole in the bottom. Find the work needed to raise the bucket to the platform. (Use $g = 9.8 \frac{m}{s^2}$.)
