

Show your work for full credit.

TA _____

1. (10 points) Use the Taylor coefficient formula to find the Taylor series **centered at $x = 2$** for $f(x) = 1/x^2$.

2. (10 points) Use Taylor Series to approximate $\int_0^1 e^{-x^2} dx$ with error less than 0.01. Use as few terms as are necessary and explain how you know you have used enough terms.

3. (6 points) Find a set of parametric equations for a circle of radius 2 centered at (3,4) and traveled once around, counterclockwise from the top.

4. A closed curve that intersects itself only at the endpoints is defined parametrically by

$$x = t^3 - 3t, \quad y = 3t^2, \quad -\sqrt{3} \leq t \leq \sqrt{3}.$$

- (a) (6 points) Determine whether the curve is traveled clockwise or counterclockwise. (Justify your answer!) Then derive an integral representing the area enclosed by the curve. You need not compute the integral.

- (b) (8 points) Determine the perimeter of the curve. The exact answer is required for full credit.

5. (6 points) Compute $\lim_{x \rightarrow 0} \frac{\sin(x^3) - x^3}{x^9}$.

6. (6 points) Determine the point(s) for which the curve $x=t^3-12t$, $y=3t^4-4t^3-12t^2$ has a vertical tangent.

7. (8 points) A cone of radius r and height h is created by rotating the line segment from $(0,0)$ to (h,r) around the x -axis. Derive the surface area formula for a cone using calculus.